

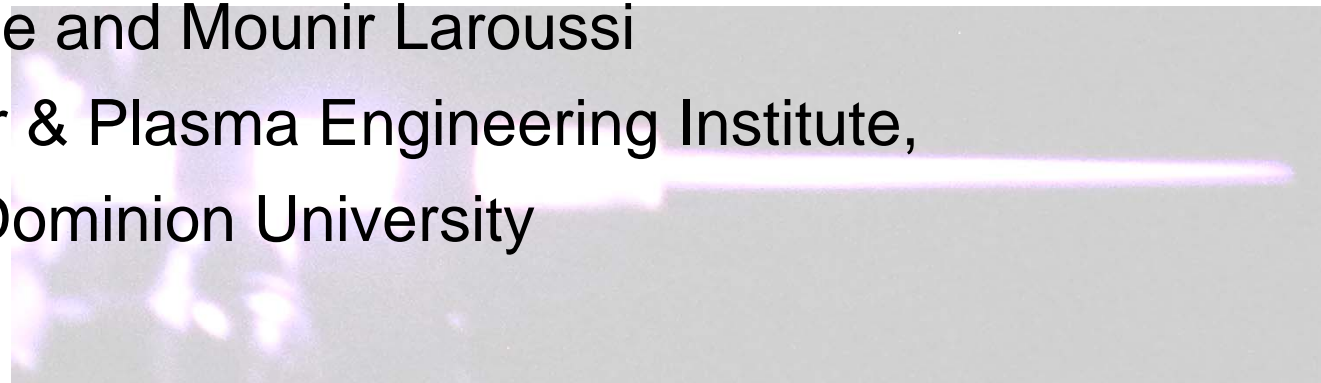
# Finite Element Analysis of Ring-shaped Emission Profile in Plasma Bullet

Yuki Sakiyama and David B. Graves,

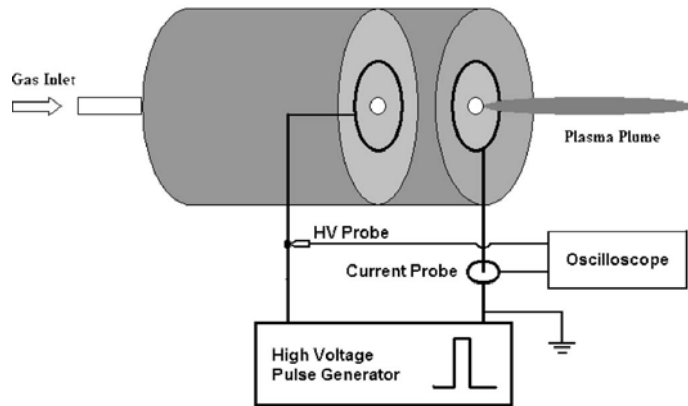
Department of Chemical Engineering,  
University of California, Berkeley

Julien Jarrige and Mounir Laroussi

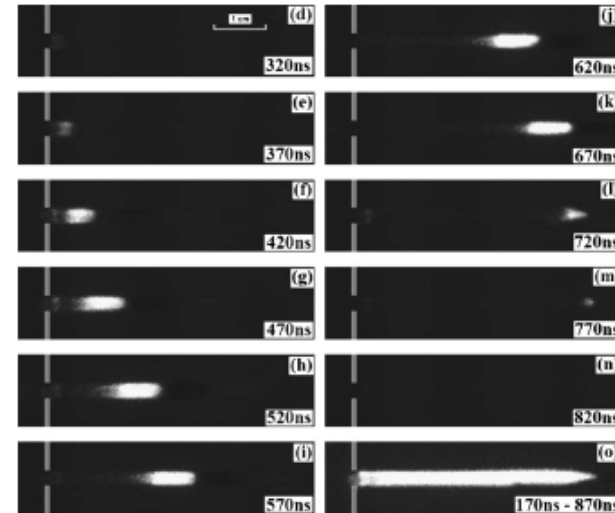
Laser & Plasma Engineering Institute,  
Old Dominion University



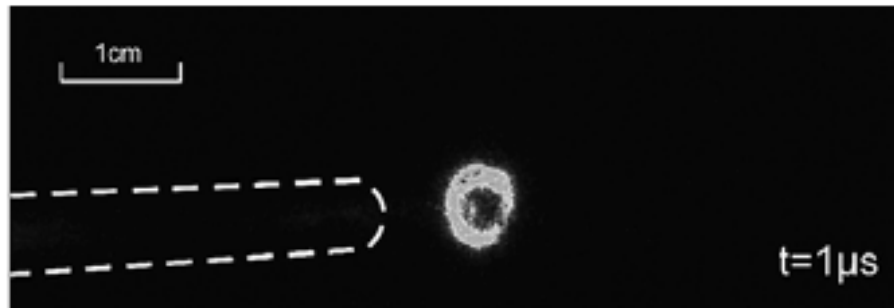
# Introduction



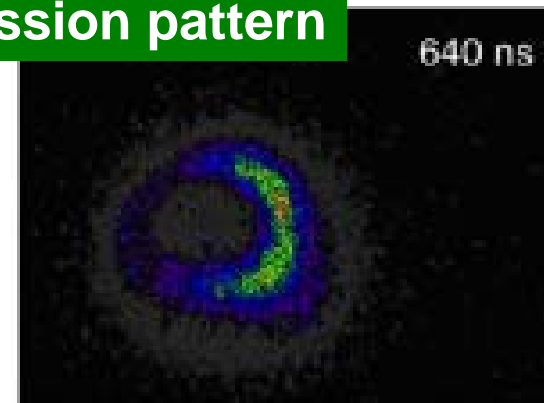
X.-P. Lu, et al., *J. Appl. Phys.* **100** (2006) 063302.



## Observed ring-shaped emission pattern



M. Teschke et al,  
*IEEE Trans. Plasma Sci.* **33** (2005) 310.



N. Merciam-Bourdet et al,  
*J. Phys. D* **42** (2009) 055207.

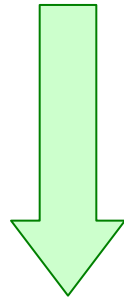
# Model description: the strategy

- He: 7 slpm
- 7 kV pulse excitation
- 8 kHz repetition

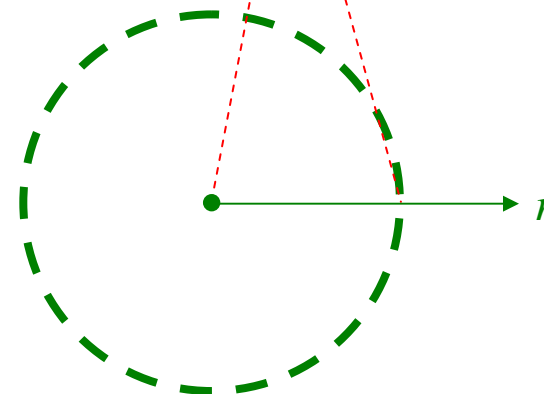
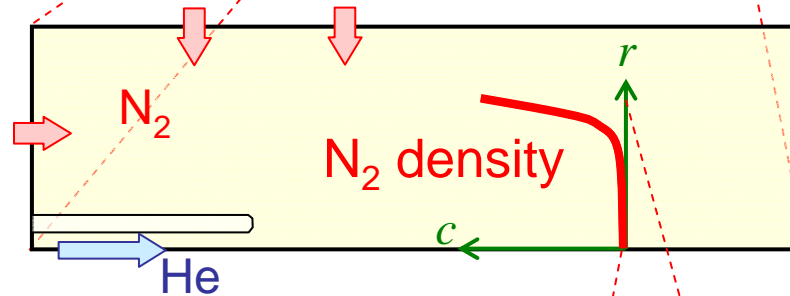


**2D steady state  
neutral gas flow**

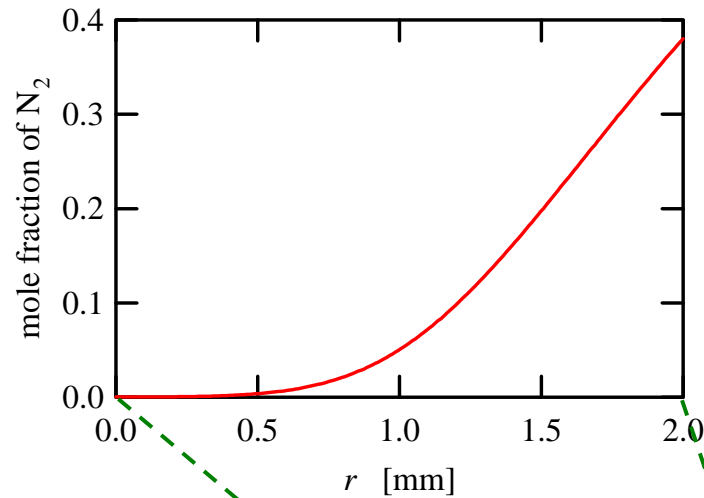
N<sub>2</sub> density  
distribution



**1D plasma dynamics  
in cylindrical coordinates  
(cross sectional view)**



# Model description: 2-D steady state gas flow



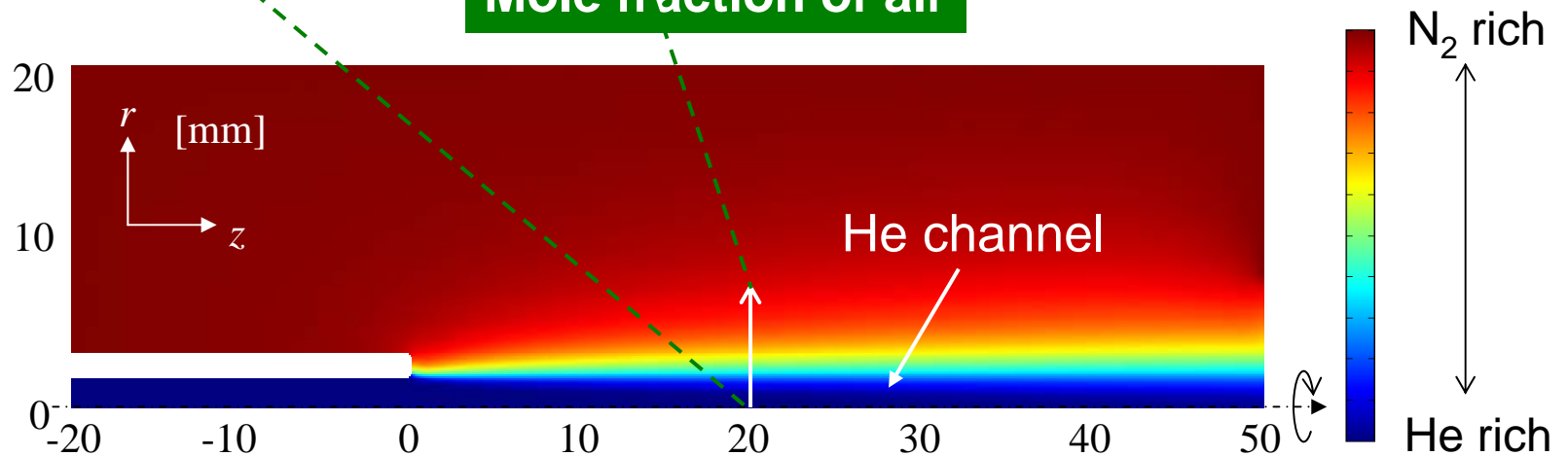
## governing N-S equation

$\rho \mathbf{u} \cdot \nabla \mathbf{u} = -\nabla p$  : total mass continuity

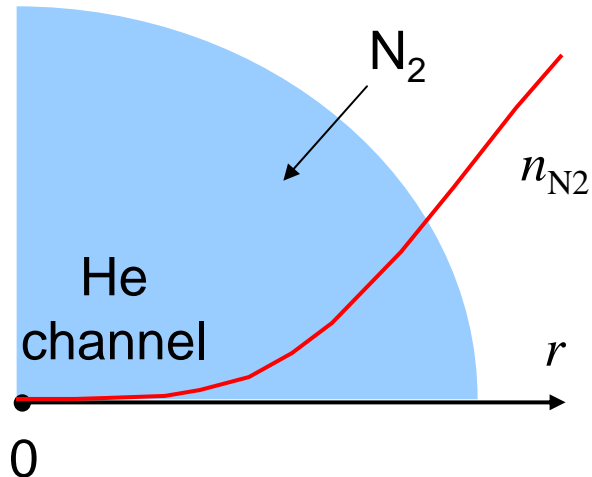
$\rho \mathbf{u} \cdot \nabla \mathbf{u} = -\nabla p$  : continuity for  $N_2$

$\rho \mathbf{u} \cdot \nabla \mathbf{u} = -\nabla p$  : total momentum continuity

## Mole fraction of air



# Model description: 1-D plasma dynamics



- species: e, He<sup>\*</sup>, He<sub>2</sub><sup>\*</sup>, He<sup>+</sup>, He<sub>2</sub><sup>+</sup>, N<sub>2</sub><sup>\*</sup>, N<sub>2</sub><sup>+</sup>
- rate coefficients: from local Boltzmann equation (local field and N<sub>2</sub> concentration)
- pressure: 1 atm
- temperature: 300 K
- solver: COMSOL and Matlab

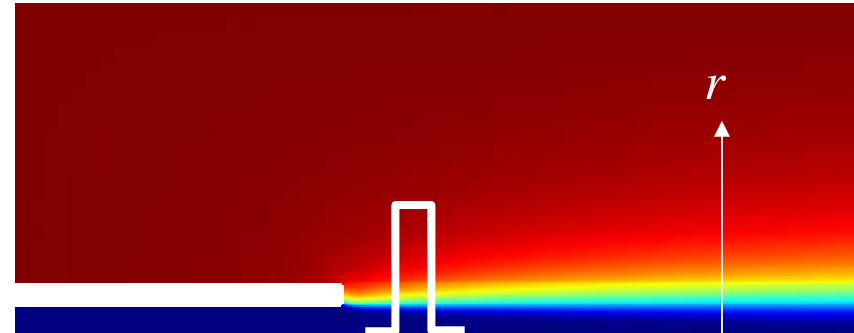
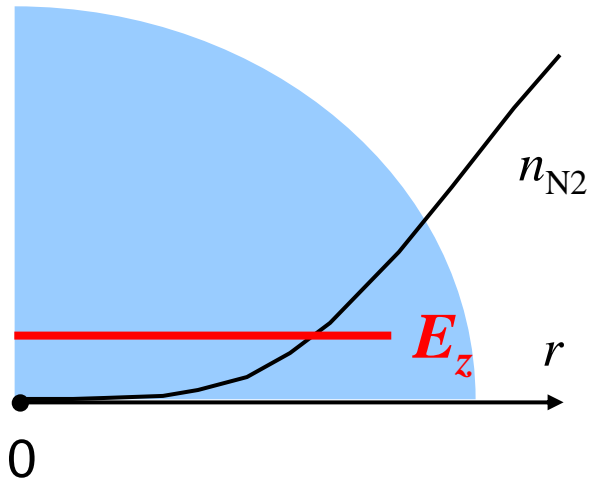
## Fluid model with local field approximation

$$\frac{\partial n_i}{\partial t} + \frac{1}{r} \frac{\partial(r\Gamma_i)}{\partial r} = S_i \quad (\text{mass continuity})$$

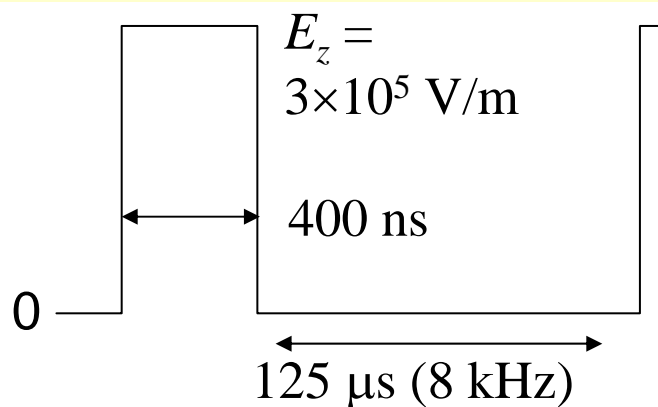
$$\Gamma_i = \text{sgn}(q_i) n_i \mu_i E_r - D_i \frac{\partial n_i}{\partial r} \quad (\text{drift-diffusion})$$

$$\epsilon_0 \frac{1}{r} \frac{\partial(rE_r)}{\partial r} = \sum_i q_i n_i \quad (\text{Poisson's eq. in r-direction})$$

# Model description: 1-D plasma dynamics -2



**Given electric field (not self-consistent!)**

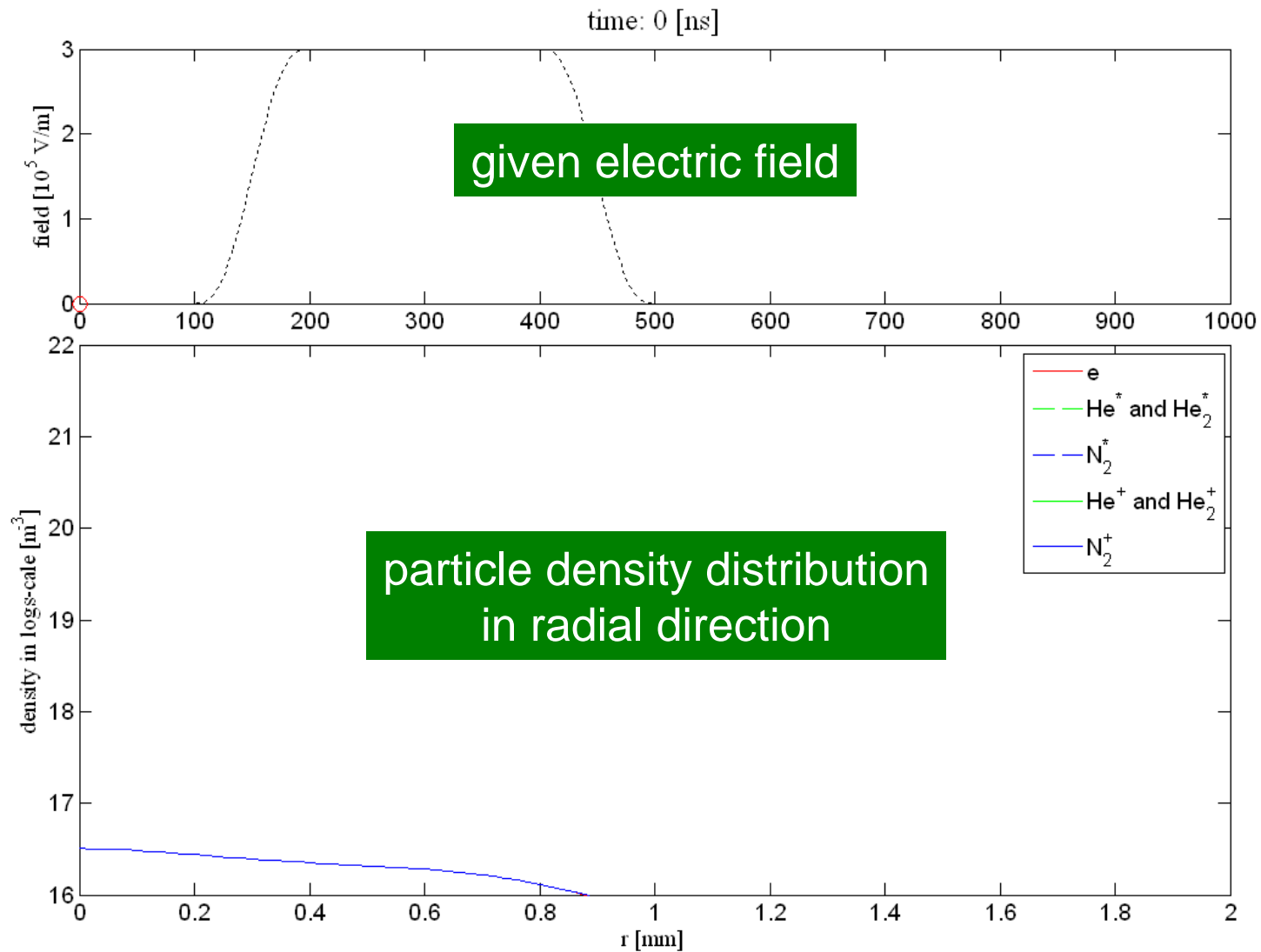


$$|\mathbf{E}| = \sqrt{|E_r|^2 + |E_z|^2}$$

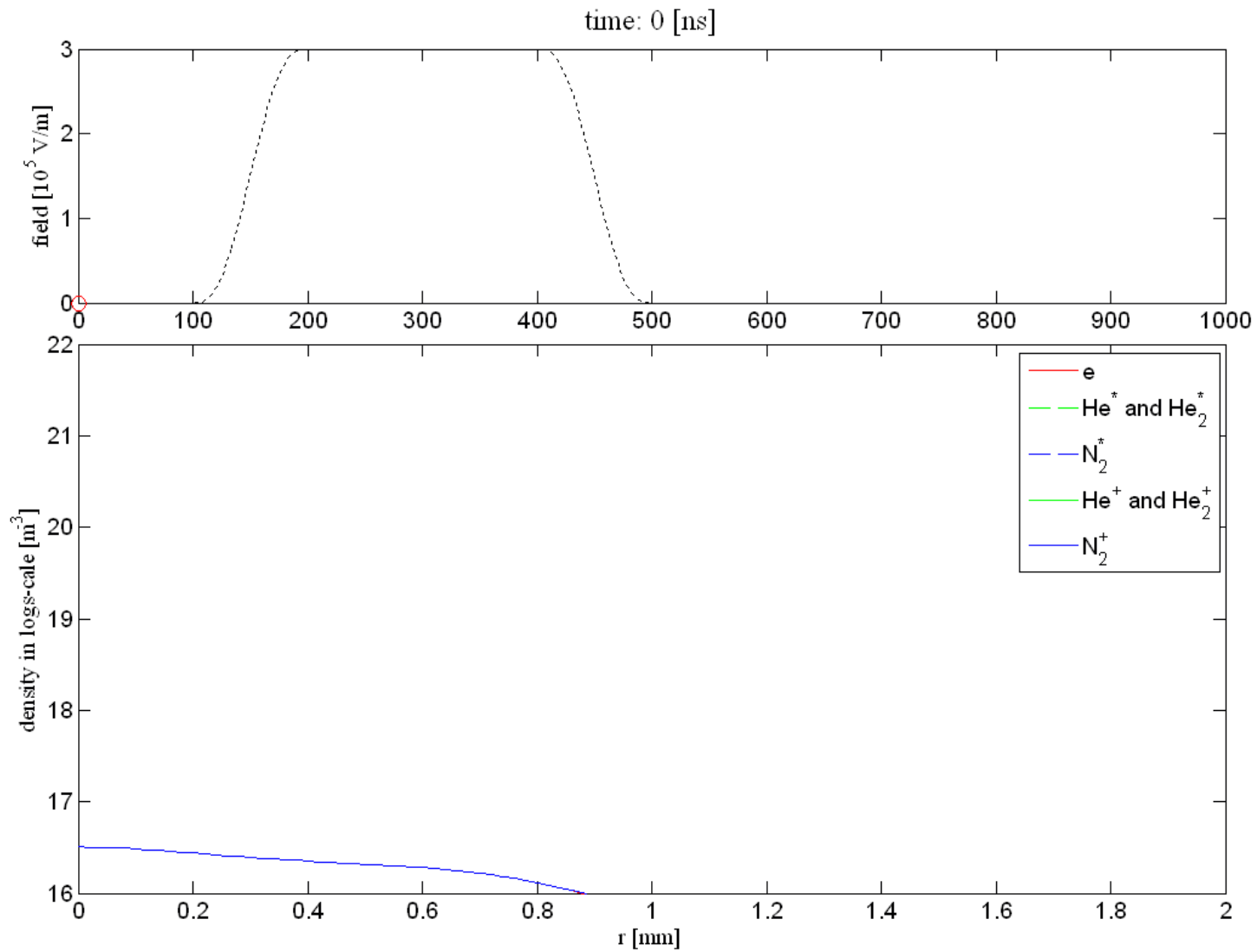
Poisson's eq.      given

reaction rate:  $k = f(|\mathbf{E}|)$

# Results: plasma dynamics ( $z = 20$ mm)



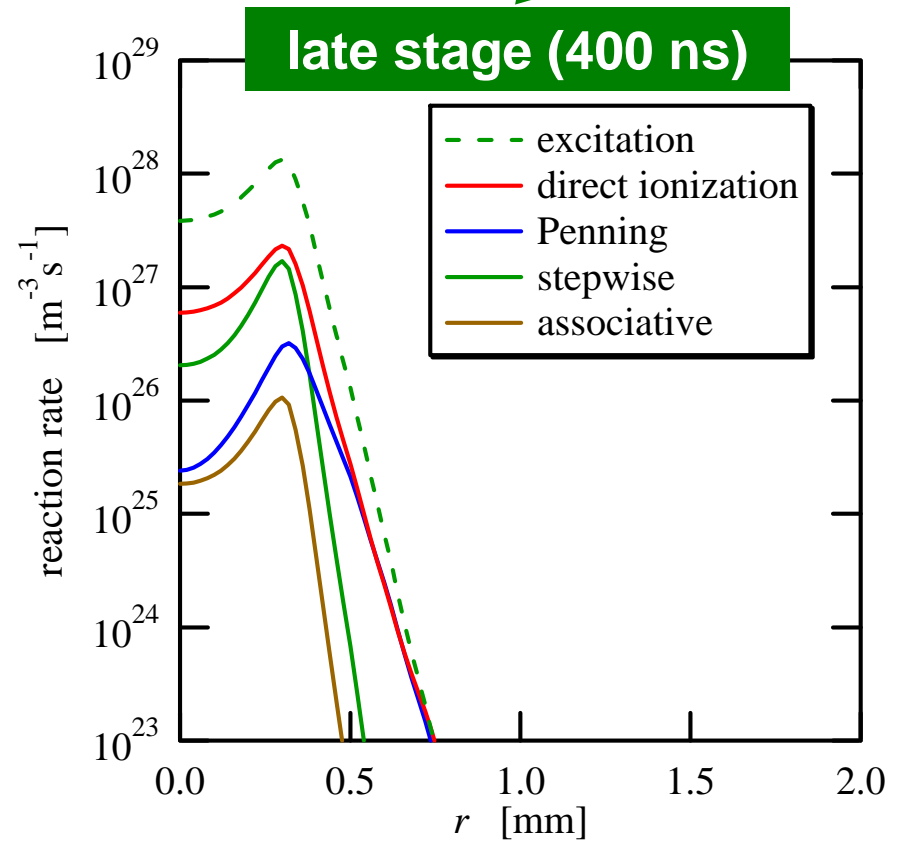
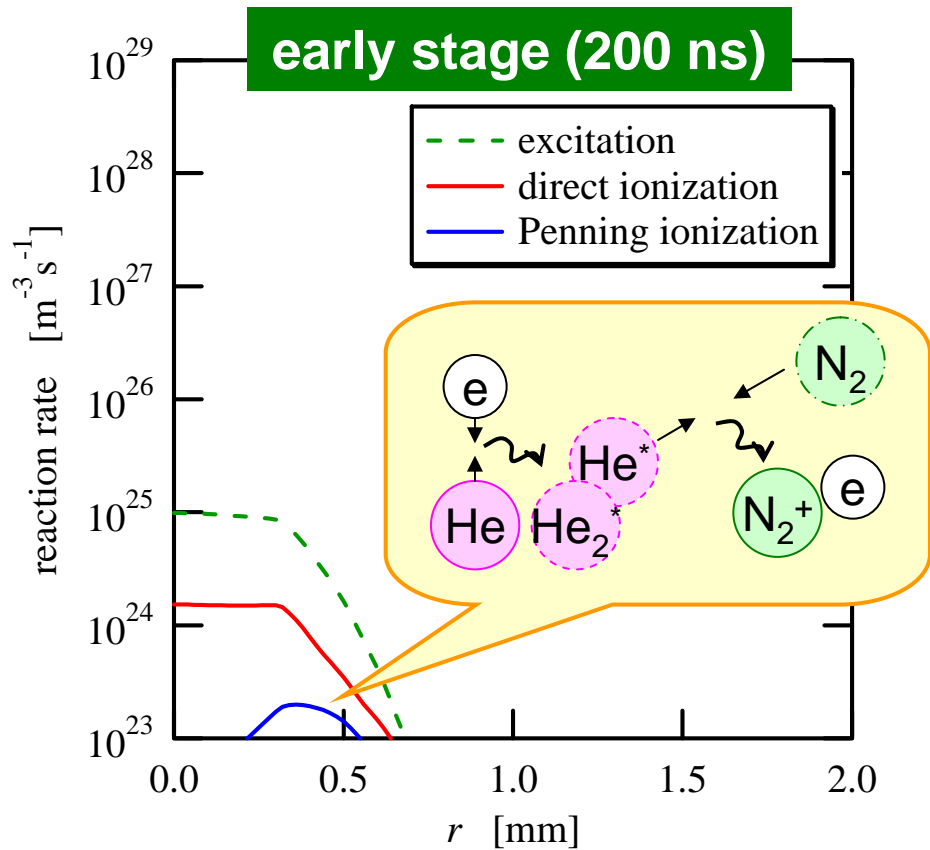
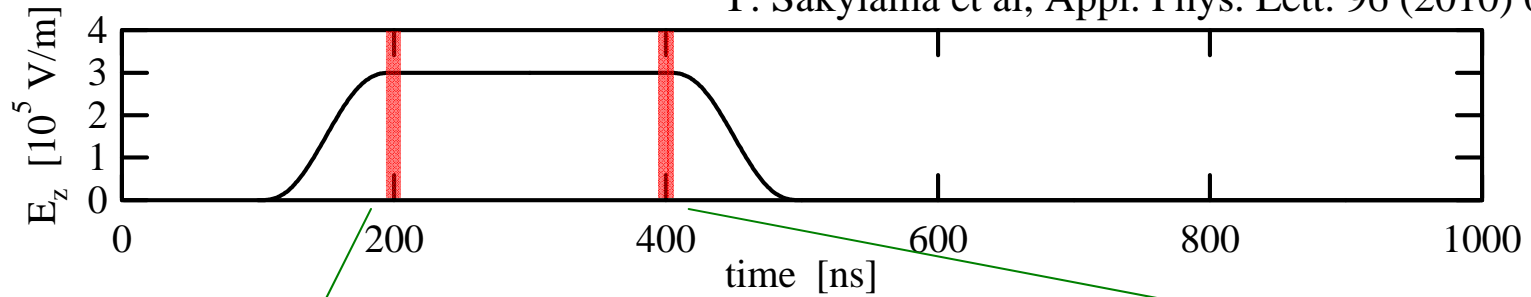
# Results: plasma dynamics ( $z = 20$ mm)



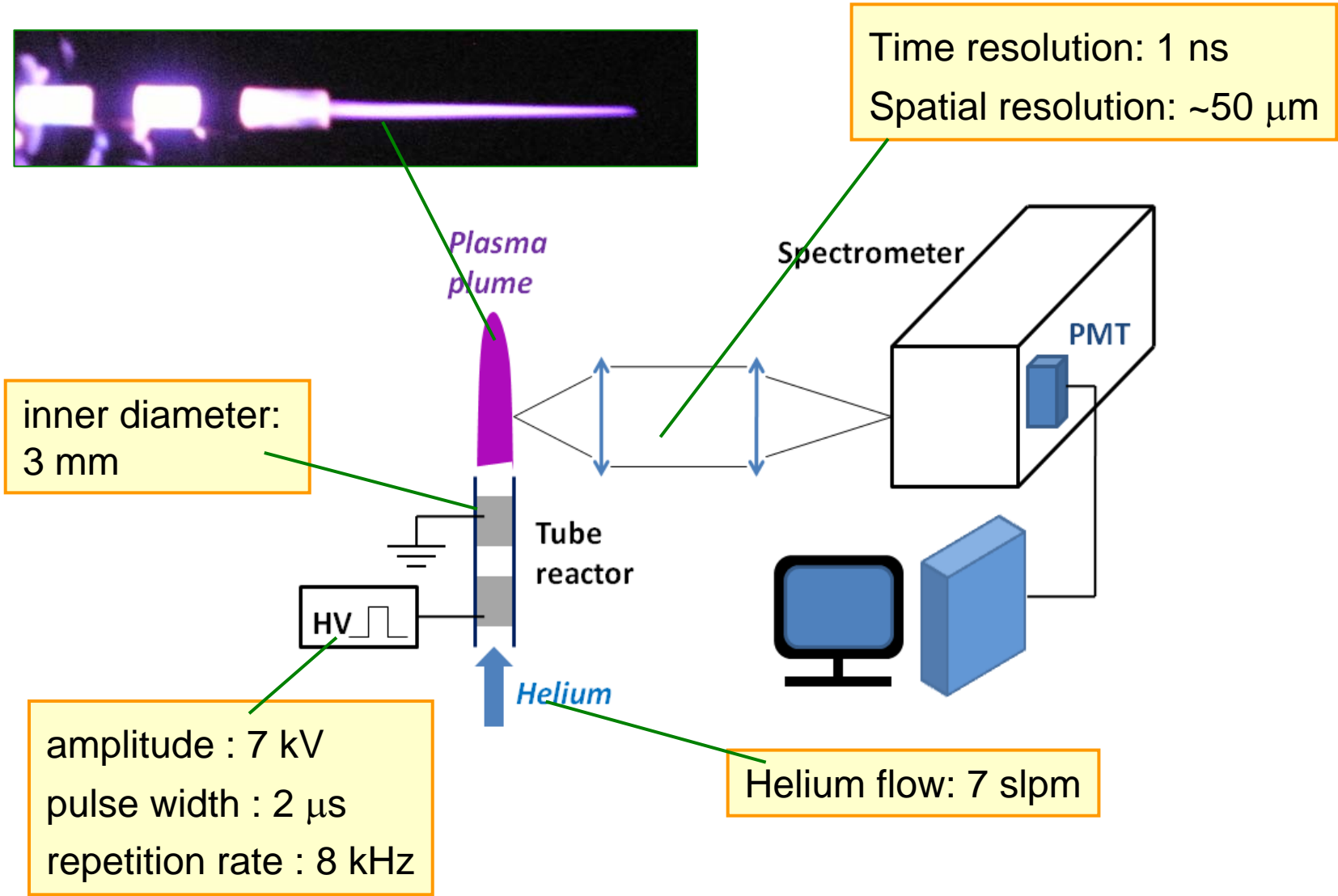


# Results: ionization mechanisms ( $z = 20$ mm)

Y. Sakyama et al, Appl. Phys. Lett. 96 (2010) 041501

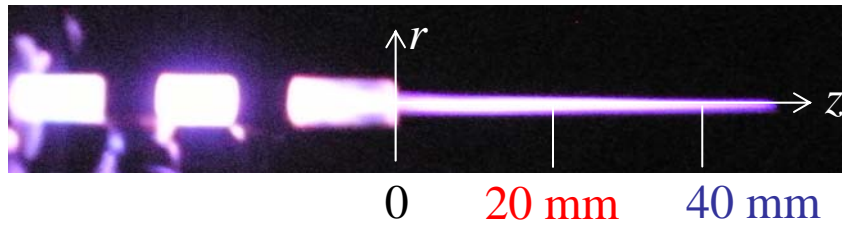


# Experiments: time and spatially-resolved OES

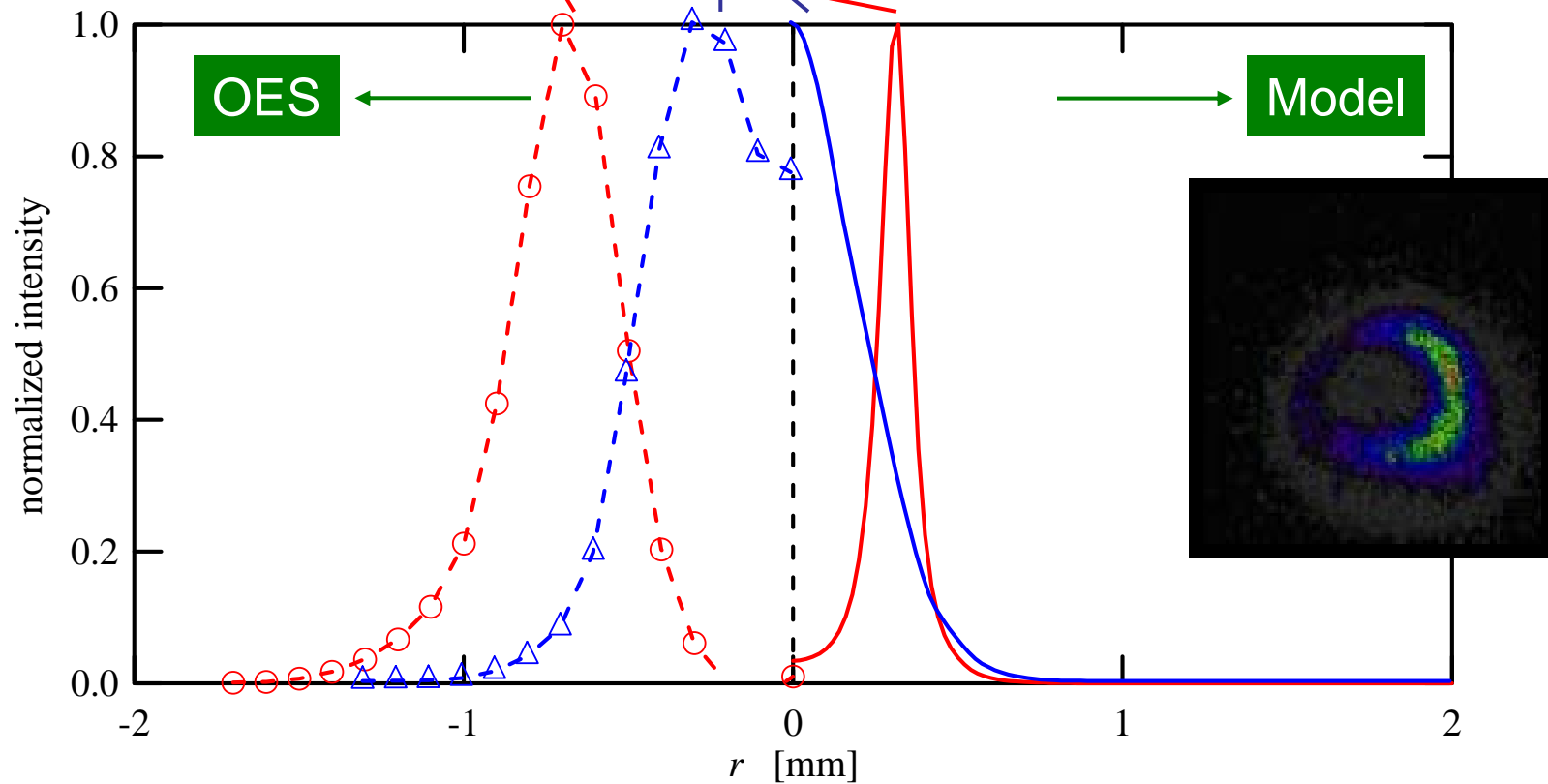


# Results: N<sub>2</sub> SPS profile in radial direction

Y. Sakyama et al, Appl. Phys. Lett. 96 (2010) 041501

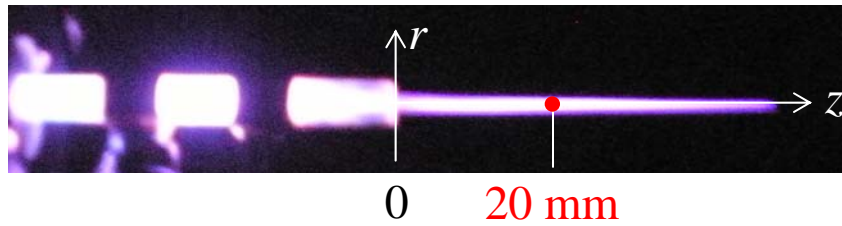


integration time for OES:  
100 ms (800 bullets)

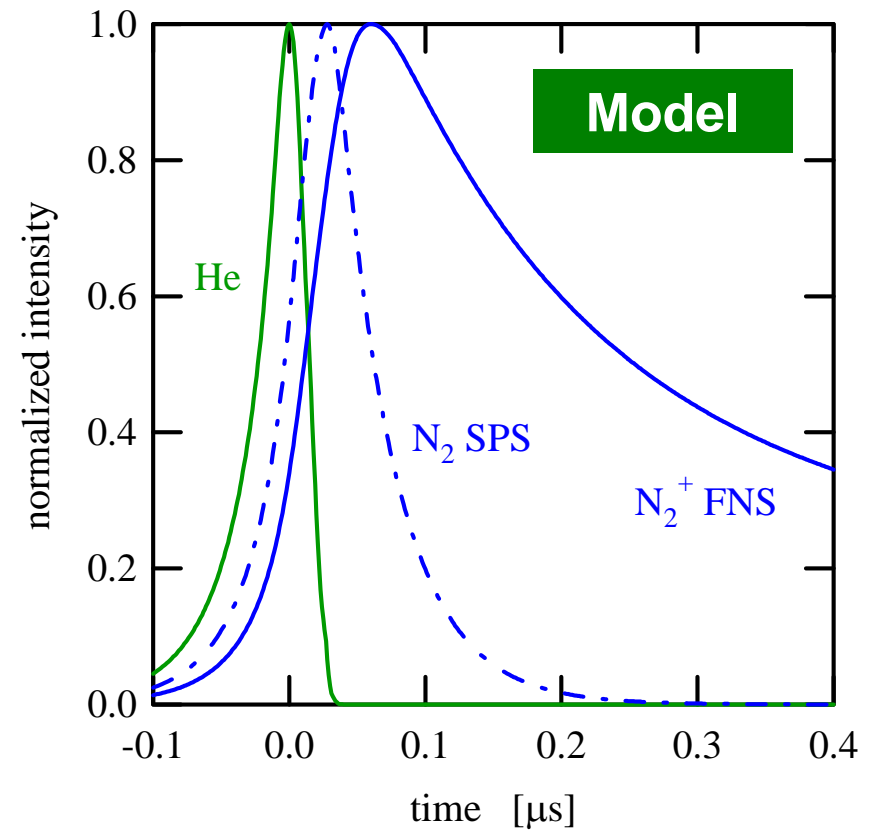
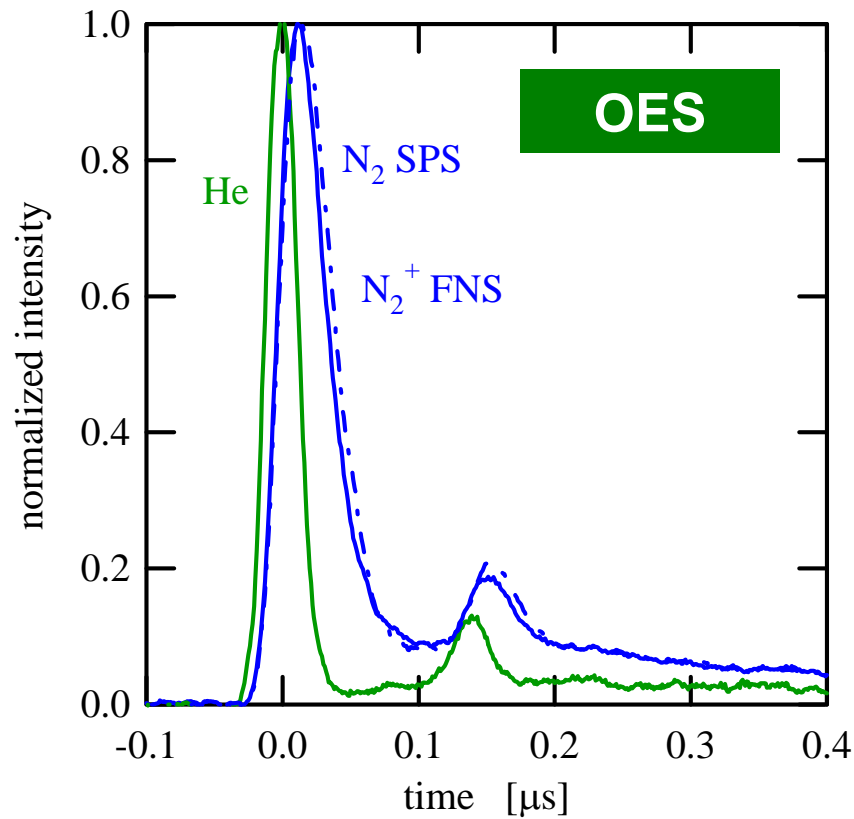


# Results: time-development of emission profile

Y. Sakyama et al, Appl. Phys. Lett. 96 (2010) 041501



$N_2$  ( $C^3\Pi_u$ ): SPS at 337.1 nm  
 $N_2^+$  ( $B^2\Sigma_u^+$ ): FNS at 391.2 nm  
He: 706.5 nm



# Concluding Remarks

---

1. We have developed a one-way coupling model between neutral gas flow and plasmas for modeling of the plasma bullet.
2. The ring-shaped profile is **initiated by Penning ionization** between helium metastables and background nitrogen at the early stage.
3. **The diameter of the ring decreases as the bullet propagates** due to quenching by air. This agrees with our OES measurement.